

# Atomic Energy Central School No 4

## Rawatbhata

### CLASS 11 - PHYSICS

#### MULTIPLE CHOICE EXAMINATION JANUARY 2019-20

Time Allowed: 1 hour

Maximum Marks: 40

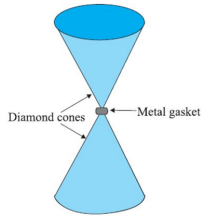
#### Section A

1. According to Hooke's law [1]
  - a) For small deformations the stress and strain are proportional to each other
  - b) For small deformations the stress is proportional to square of strain
  - c) For small deformations the stress and strain are inversely proportional to each other
  - d) For large deformations the stress and strain are proportional to each other
2. A specimen of oil having an initial volume of  $600 \text{ cm}^3$  is subjected to a pressure increase of  $3.6 \times 10^6 \text{ Pa}$  and the volume is found to decrease by  $0.45 \text{ cm}^3$  what is the bulk modulus of the material? [1]
  - a)  $4.4 \times 10^9 \text{ Pa}$
  - b)  $5.0 \times 10^9 \text{ Pa}$
  - c)  $4.8 \times 10^9 \text{ Pa}$
  - d)  $4.6 \times 10^9 \text{ Pa}$
3. How much should the pressure on a litre of water be changed to compress it by 0.10 percent? [1]

Bulk modulus of water 2.2 GPa

  - a)  $2.4 \times 10^6 \text{ N/m}^2$
  - b)  $2.2 \times 10^6 \text{ N/m}^2$
  - c)  $2.6 \times 10^6 \text{ N/m}^2$
  - d)  $2.0 \times 10^6 \text{ N/m}^2$
4. A specimen of oil having an initial volume of  $600 \text{ cm}^3$  is subjected to a pressure increase of  $3.6 \times 10^6 \text{ Pa}$  and the volume is found to decrease by  $0.45 \text{ cm}^3$  what is the compressibility of the material? [1]
  - a)  $2.3 \times 10^{-10} \text{ Pa}^{-1}$
  - b)  $2.1 \times 10^{-10} \text{ Pa}^{-1}$
  - c)  $1.7 \times 10^{-10} \text{ Pa}^{-1}$
  - d)  $1.9 \times 10^{-10} \text{ Pa}^{-1}$
5. Four identical hollow cylindrical columns of mild steel support a big structure of mass 50,000 kg. The inner and outer radii of each column are 30 and 60 cm respectively. Assuming the load distribution to be uniform, calculate the compression strain of each column. . Take Young's modulus of steel as  $20 \times 10^{10} \text{ Pa}$  [1]
  - a)  $2.95 \times 10^{-6}$
  - b)  $3.1 \times 10^{-6}$
  - c)  $3.0 \times 10^{-6}$
  - d)  $2.18 \times 10^{-6}$
6. Anvils made of single crystals of diamond, with the shape as shown in Figure, are used to investigate behaviour of materials under very high pressures. Flat faces at the narrow end of the anvil have a diameter of 0.50 mm, and the wide ends are subjected to a compression force [1]

of 50,000 N. What is the pressure at the tip of the anvil?



- a)  $2.1 \times 10^{11}$  Pa
- b)  $2.5 \times 10^{11}$  Pa
- c)  $2.9 \times 10^{11}$  Pa
- d)  $3.2 \times 10^{11}$  Pa

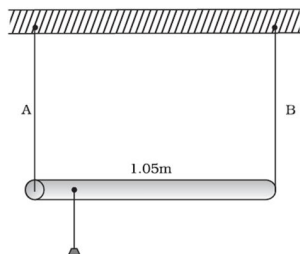
7. The importance of the elastic behavior of materials is [1]

- a) that it gives methods for understanding materials
- b) that it is useful in building sling shots
- c) that it is useful in making springs
- d) that it enables a safe and sound design of bridges, buildings, machinery parts.

8. What is the density of water at a depth where pressure is 80.0 atm, given that its density at the surface is  $1.03 \times 10^3 \text{ kg m}^{-3}$ ? [1]

- a)  $1.054 \times 10^3 \text{ kg/m}^3$
- b)  $1.074 \times 10^3 \text{ kg/m}^3$
- c)  $1.094 \times 10^3 \text{ kg/m}^3$
- d)  $1.034 \times 10^3 \text{ kg/m}^3$

9. A rod of length 1.05 m having negligible mass is supported at its ends by two wires of steel (wire A) and aluminum (wire B) of equal lengths as shown in Figure. The cross-sectional areas of wires A and B are  $1.0 \text{ mm}^2$  and  $2.0 \text{ mm}^2$ , respectively. At what point along the rod should a mass  $m$  be suspended in order to produce equal stresses? Take Young's modulus of steel as 200 GPa, for aluminum 70 GPa [1]



- a) 0.8 m from steel wire
- b) 0.7 m from steel wire
- c) 0.6 m from steel wire
- d) 0.9 m from steel wire

10. When a solid is deformed, [1]

- a) only the atoms or molecules of the surface move from their equilibrium position
- b) only the atoms or molecules at some points move from their equilibrium position
- c) the atoms or molecules do not move from their equilibrium position
- d) all the atoms or molecules are displaced from their equilibrium positions causing a change in inter atomic (or intermolecular) distances.

11. Water rises to a height of 16.3 cm in a capillary of height 18 cm above the water level. If the [1]

tube is suddenly cut at a height of 12 cm

- a) the height of the water in the capillary will be 10.3 cm
- b) water will stay at a height of 12 cm in the capillary tube
- c) water will come as a fountain from the capillary tube
- d) water will flow down the sides of the capillary tube

12. According to Pascal's law for transmission of fluid pressure external pressure applied on any part of a fluid contained in a vessel is \_\_\_\_\_ in all directions [1]

- a) transmitted and increased
- b) transmitted undiminished and equally
- c) not transmitted
- d) transmitted and decreased

13. in laminar flow [1]

- a) adjacent layers of fluid move in circle crossing each other each other and the flow is steady
- b) adjacent layers of fluid do not slide smoothly past each other and the flow is unsteady
- c) adjacent layers of fluid slide smoothly past each other and the flow is steady
- d) adjacent layers of fluid slide smoothly past each other and the flow is unsteady

14. A parrot is in a wire cage, which is hanging from a spring balance. Initially the parrot sits in the cage and in the second instant the parrot flies inside the cage, the reading of the balance will be [1]

- a) Lesser when the parrot flies in the cage
- b) None of these
- c) Greater when the parrot flies in the cage
- d) Remain unchanged

15. Two match sticks are laid side by side on the surface of water. When a drop of light oil on the end of a third match stick is touched to the surface film between the two floating sticks, the two match sticks [1]

- a) will move apart rapidly
- b) will remain as they are
- c) will come closer
- d) will be joined

16. At large flow velocities the flow of a fluid becomes [1]

- a) viscous
- b) turbulent
- c) compressible
- d) laminar

17. Two bodies are in equilibrium when suspended in water from the arms of a balance. The mass of one body is 36 gm and its density is 9 gm/cc. If the mass of the other is 48 gm, its density in  $gm/cm^3$  is [1]

- a) 3.0
- b) 4/3
- c) 3/2
- d) 5

18. A liquid drop of radius R is broken up into N small droplets. The work done is proportional to [1]



container of mercury of sp. gr. 13.6?

- a) 0.78
- b) 0.47
- c) 0.53
- d) 0.75

28. It is easier to spray water to which soap is added, because **[1]**

- a) Addition of soap to water increases surface tension of water
- b) Addition of soap to water decreases surface tension of water
- c) Addition of soap to water makes surface tension of water zero
- d) Addition of soap to water increases its density

29. A tank with a square base of area  $2.0\text{ m}^2$  is divided into two compartments by a vertical partition in the middle. There is a small hinged door of face area  $20\text{ cm}^2$  at the bottom of the partition. Water is filled in one compartment and an acid, of relative density 1.7, in the other, both to a height of 4m. If  $g = 10\text{ ms}^{-2}$  the force necessary to keep the door closed is **[1]**

- a) 80.88 N
- b) 20.92 N
- c) 40.52 N
- d) 54.88 N

30. In a hydraulic lift the force applied on the smaller cylinder of area  $A_1$  is  $F_1$ . If the area of the larger cylinder is  $A_2$  the maximum weight that can be lifted is **[1]**

- a)  $F_1$
- b)  $\frac{A_1}{A_2} F_1$
- c)  $F_1 A_2$
- d)  $\frac{A_2}{A_1} F_1$

31. The unit of surface tension in S.I units is given by **[1]**

- a) dynes per cm
- b) dynes per  $\text{cm}^2$
- c) Newtons per meter<sup>2</sup>
- d) Newtons per meter

32. The height of mercury column in a simple barometer is  $h$ . As tube is inclined to the vertical at an angle  $\alpha$  the length of the mercury column along the length of the tube is  $l$ , then **[1]**

- a)  $l = h/\cos\alpha$
- b)  $l = h \sin\alpha$
- c)  $l = h \cos\alpha$
- d)  $l = h$

33. An air bubble of radius  $r$  is formed inside a tank of water at depth  $h$ . The atmospheric pressure is equal to a water column of height  $H$ . the pressure inside the bubble is **[1]**

- a)  $\rho g(h + H) + \frac{T}{r}$
- b)  $\rho g(h + H) + \frac{8T}{r}$
- c)  $\rho g(h + H) + \frac{4T}{r}$
- d)  $\rho g(h + H) + \frac{2T}{r}$

34. A soap bubble has radius  $r$  and the surface tension of the soap film is  $T$ . The energy needed to double the diameter of the bubble without change of temperature is **[1]**

- a)  $8\pi r^2 T$
- b)  $4\pi r^2 T$
- c)  $12\pi r^2 T$
- d)  $14\pi r^2 T$

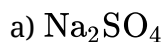
35. According to Pascal's Law the **[1]**

- a) pressure in a fluid at rest is the same at all points if they are at the same
- b) pressure in a fluid at rest is the same at all points if they are at different

- height
- heights
- c) pressure in a fluid increases with temperature
- d) pressure in a fluid decreases with temperature
36. The stream line in a flow is [1]
- a) a curve whose perpendicular at any point is in the direction of the fluid velocity at that point
- b) a curve which shows all points of equal pressure
- c) a curve whose tangent at any point is in the direction of the fluid velocity at that point
- d) a curve which shows all points of equal velocity
37. A raft of wood of density  $600\text{kg/m}^3$  and mass 120 kg floats in water. How much weight can be put on the raft to make it just sink? [1]
- a) 200kg
- b) 40kg
- c) 80kg
- d) 120kg
38. Pressure applied to an enclosed fluid is [1]
- a) Increased and applied to every part of the fluid
- b) Diminished and transmitted to the wall of the container
- c) Increased in proportion to the mass of the fluid and then transmitted
- d) Transmitted unchanged to every portion of the fluid and walls of the containing vessel
39. A wooden cube just floats inside water when a 200gm mass is placed on it. When the mass is removed, the cube is 2 cm above the water level. The size of the cube is [1]
- a) 15 cm
- b) 5 cm
- c) 20 cm
- d) 10 cm
40. Density is defined as [1]
- a) volume of 1 kg of the material
- b) mass per unit volume
- c) volume per unit mass
- d) volume of 10 kg of the material



used for textile industry?



48. Which of the following are the correct reasons for anomalous behaviour of lithium? [1]
- a) Exceptionally low ionisation enthalpy                      b) Low degree of hydration
- c) Exceptionally small size of its atom                      d) Its low polarising power
49. Alkaline earth metals have large size of the atoms. Therefore, they shows [1]
- a) low electopositivity                      b) low ionization enthalpies
- c) low hydration enthalpies                      d) low nuclear charge
50. Cement is an industrially important compound of [1]
- a) Potassium                      b) Calcium
- c) Magnesium                      d) Sodium
51. Magnesium do not impart any colour to the flame because [1]
- a) The electrons in magnesium are too strongly bound to get excited                      b) Low absorption of light energy
- c) The electrons in magnesium are too loosly bound to get excited                      d) Low thermal conductivities
52. Which of the following is not a peroxide? [1]
- a)  $\text{Na}_2\text{O}_2$                       b)  $\text{CrO}_5$
- c)  $\text{BaO}_2$                       d)  $\text{KO}_2$
53. Alkali metals react with water vigorously to form hydroxides and dihydrogen. Which of the following alkali metals reacts with water least vigorously? [1]
- a) Na                      b) K
- c) Cs                      d) Li
54. Which of the following is used in photo-electric cells? [1]
- a) K                      b) Na
- c) Cs                      d) Li
55. Lithium shows a diagonal relationship with [1]
- a) silicon                      b) magnesium
- c) nitrogen                      d) sodium
56. Which of the alkali metal is having least melting point? [1]
- a) Cs                      b) Na
- c) Rb                      d) K
57. The diagonal relationship exists between [1]



- a) Lithium and magnesium                      b) Beryllium and magnesium  
c) Lithium and beryllium                      d) Lithium and aluminium
58. The oxide of which of the following metals is amphoteric? [1]  
a) Ca    b) Mg  
c) Ba    d) Be
59. Why does the solubility of alkaline earth metal carbonates and sulphates in water decrease down the group? [1]  
a) hydration enthalpy decreases down the group                      b) size of anions being much shorterer compared to cations  
c) coordination number more than four                      d) lattice enthalpy decreases down the group
60. When Zeolite, which is hydrated sodium aluminium silicate is treated with hard water, the sodium ions are exchanged with which of the following ion(s)? [1]  
a)  $Mg^{2+}$  ions    b)  $H^{+}$  ions  
c)  $SO_4^{2-}$  ions    d)  $O^{2-}$  ions
61. Elements of which of the following group(s) of periodic table do not form hydrides. [1]  
a) Groups 7, 8, 9    b) Groups 15, 16, 17  
c) Group 14    d) Group 13
62. Water undergoes self ionization to a small extent to give [1]  
a)  $H_3O^{+}$  and  $OH^{-}$     b)  $OH^{+}$  and  $H^{-}$   
c)  $OH^{+}$  and  $OH^{-}$     d)  $H^{+}$  and  $OH^{-}$
63. Consider the reactions [1]  
(A)  $H_2O_2 + 2HI \rightarrow I_2 + 2H_2O$   
(B)  $HOCl + H_2O_2 \rightarrow H_3O + Cl + O_2$   
Which of the following statements is correct about  $H_2O_2$  with reference to these reactions?  
Hydrogen peroxide is  
a) a reducing agent in both (A) and (B)                      b) a reducing agent in (A) and oxidising agent in (B)  
c) an oxidising agent in (A) and reducing agent in (B)                      d) an oxidising agent in both (A) and (B)
64. Which of the following equations depict the oxidising nature of  $H_2O_2$ ? [1]  
a)  $2MnO_4^{-} + 6H^{+} + 5H_2O_2 \rightarrow 2Mn^{2+} + 2H_2O + 5O_2$                       b)  $2H_2O_2 \rightarrow I_2 + 2H_2O$   
c)  $2Fe^{3+} + 2H^{+} + H_2O_2 \rightarrow 2Fe^{2+} + 2H_2O$                       d)  $2KIO_3 + H_2O_2 \rightarrow KIO_3 + H_2O + O_2$
65. Which of the following statement(s) is/are correct in the case of heavy water? [1]  
a) Heavy water is more effective as solvent than ordinary water.                      b) Heavy water is used as a moderator in nuclear reactor.

- c) Heavy water has lower boiling point than ordinary water.      d) Heavy water is more unassociated than ordinary water.
66. Temporary hardness It can be removed in boiling by precipitating [1]  
 a)  $\text{Mg}(\text{HCO}_3)_2 \cdot \text{CaCO}_3$       b)  $\text{Ca}(\text{HCO}_3)_2 \cdot \text{Mg}(\text{OH})_2$   
 c)  $\text{CaCO}_3 \cdot \text{Mg}(\text{OH})_2$       d)  $\text{Mg}(\text{HCO}_3)_2 \text{Ca}(\text{HCO}_3)_2$
67. Hydrogenation of vegetable oil using nickel as catalyst gives edible fats. Choose the appropriate one given below. [1]  
 a) vanaspati      b) Cheese  
 c) sunflower oil      d) Rice bran oil
68.  $\text{H}_2\text{O}_2$  behaves as a bleaching agent because: [1]  
 a) it breaks the chemical bonds of the chromophores      b) acts as a strong reducing agent in basic media  
 c) it absorbs the visible light      d) acts as a strong reducing agent in acidic media
69. Dihydrogen can be prepared on commercial scale by different methods. In its preparation by the action of steam on hydrocarbons, a mixture of CO and  $\text{H}_2$  gas is formed. It is known as \_\_\_\_\_ [1]  
 a) Producer gas      b) Starter gas  
 c) Industrial gas      d) Water gas
70. Pure de-mineralised water is obtained by passing water through an anion exchange as a second process after passing it through a cation exchange. This makes the water [1]  
 a) basic      b) acidic  
 c) remain unchanged      d) neutral
71. Hydrogen peroxide is used as: [1]  
 a) all of these      b) a bleaching agent  
 c) a reducing agent      d) an oxidizing agent
72. Hydrogen peroxide is obtained by the electrolysis of \_\_\_\_\_. [1]  
 a) water      b) fused sodium peroxide  
 c) hydrochloric acid      d) sulphuric acid
73. On treatment of hard water with zeolite, sodium ions get exchanged with [1]  
 a)  $\text{Na}^+$  ions      b)  $\text{Ca}^{2+}$  ions  
 c)  $\text{H}^+$  ions      d)  $\text{OH}^-$
74. Which of the following statements are not true for hydrogen? [1]  
 a) It has one electron in the outermost shell.      b) It can lose an electron to form a cation which can freely exist  
 c) It forms a large number of ionic      d) It exists as diatomic molecule.



# Atomic Energy Central School No 4

## Rawatbhata

### CLASS 11 - MATHEMATICS

#### Multiple Choice Questions Examination January (2019-20)

Time Allowed: 1 hour and 30 minutes

Maximum Marks: 40

#### General Instructions:

Note: Darken the most appropriate circle on the OMR Sheet against each question .

#### Section A

81. In an ellipse the distance between its foci is 6 and its minor axis is 8 ; the eccentricity of the ellipse is [1]  
a)  $\frac{1}{\sqrt{52}}$  b)  $\frac{1}{2}$   
c)  $\frac{3}{5}$  d)  $\frac{3}{5}$
82. The parabolas  $x^2 = 4y$  and  $y^2 = 4x$  intersect [1]  
a) on the line  $x + y = 0$  b) on the line  $y = x$   
c) none of these d) in a unique point
83. The equation of the directrix of the parabola  $x^2 = -4ay$  is [1]  
a)  $y - a = 0$  b)  $x - a = 0$   
c)  $x + a = 0$  d)  $y + a = 0$
84. The equation  $x^2 + 3y^2 - 9x + 2y + 1 = 0$  represents [1]  
a) a parabola b) a circle  
c) a hyperbola d) an ellipse
85. The length of latus rectum of an ellipse is one-third of its major axis. Its eccentricity would be [1]  
a)  $\frac{2}{3}$  b)  $\sqrt{\frac{2}{3}}$   
c)  $\frac{1}{\sqrt{3}}$  d)  $\frac{1}{\sqrt{2}}$
86. The eccentricity of the conic  $9x^2 - 16y^2 = 144$  is [1]  
a)  $\frac{5}{4}$  b)  $\frac{4}{5}$   
c)  $\frac{4}{3}$  d)  $\sqrt{7}$
87. The radius of the circle  $3x(x - 2) + 3y(y + 1) = 4$  is [1]  
a) 3 b)  $\sqrt{\frac{15}{4}}$   
c)  $\sqrt{\frac{31}{12}}$  d) 2
88. The ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1, b^2 = a^2$  is a [1]  
a) a hyperbola b) none of these.

- c) horizontal ellipse  
d) vertical ellipse
89. The centre of a circle passing through the points (0, 0), (1, 0) and touching the circle  $x^2 + y^2 = 9$  is [1]  
 a)  $(\frac{1}{2}, -\sqrt{2})$   
 b)  $(\frac{1}{2}, \frac{1}{2})$   
 c)  $(\frac{1}{2}, -\sqrt{2})$   
 d)  $(\frac{1}{2}, \frac{3}{2})$
90. The eccentricity 'e' of a parabola is [1]  
 a) Zero  
 b) More than 1  
 c) Equal to 1  
 d) Less than 1
91. The equations  $x = a \cos \theta, y = b \sin \theta, 0 \leq \theta < 2\pi, a \neq b$ , represent [1]  
 a) a parabola  
 b) an ellipse  
 c) a hyperbola  
 d) a circle
92. The vertex of the parabola  $y^2 = 4a(x+a)$  is [1]  
 a) (a, 0)  
 b) (-a, 0)  
 c) (0, 0)  
 d) (0, a)
93. The eccentricity of the hyperbola  $x^2 - y^2 = 9$  is [1]  
 a) less than 1  
 b) none of these  
 c)  $\sqrt{2}$   
 d) 1
94. If the length of the major axis of an ellipse is three times the length of its minor axis, its eccentricity is [1]  
 a)  $\frac{1}{\sqrt{2}}$   
 b)  $\frac{2\sqrt{2}}{3}$   
 c)  $\frac{1}{3}$   
 d)  $\frac{1}{\sqrt{3}}$
95. The radius of the circle passing through the foci of the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$  and having its centre at (0, 3) is [1]  
 a)  $\frac{7}{2}$   
 b)  $\sqrt{12}$   
 c) 3  
 d) 4
96. The equation  $\vec{r} = \lambda \hat{i}$  represents [1]  
 a) the Z axis  
 b) the Y axis  
 c) the YOZ plane  
 d) the X axis
97. The equations of y axis are [1]  
 a)  $y = 0, z = 0$   
 b)  $x = 0, z = 0$   
 c)  $x = 0, y = 0, z = 0$   
 d)  $x = 0, y = 0$
98. The points (1, 1, 0), (0, 1, 1), (1, 0, 1), and (2/3, 2/3, 2/3) are [1]  
 a) none of these  
 b) coplanar  
 c) non coplanar  
 d) the vertices of a parallelogram
99. The plane XOZ divides the join of (1, -1, 5) and (2, 3, 4) in the ratio k : 1, then the value of k [1]

is

- a) 3  
c) - 3
- b)  $1/3$   
d)  $-1/3$

100. The ratio in which the line joining  $(2, 4, 5)$   $(3, 5, -4)$  is divided by the YZ – plane is [1]  
a) it is  $4 : -3$   
b) it is  $3 : 2$   
c) it is  $2 : 3$   
d) it is  $-2 : 3$
101. The area of the triangle whose vertices are  $(1, 2, 3)$ ,  $(2, 5, -1)$ ,  $(-1, 1, 2)$  is (sq. units) [1]  
a) 145  
b) 165  
c) 150  
d)  $\frac{\sqrt{155}}{2}$
102. The points A  $(0, 2, 0)$ , B  $(\sqrt{3}, 1, 0)$ , and C  $(\frac{1}{\sqrt{3}}, 1, \frac{2\sqrt{2}}{\sqrt{3}})$  are the vertices of [1]  
a) a scalene triangle  
b) none of these  
c) an equilateral triangle  
d) an isosceles triangle
103. The plane  $x + y = 0$  is [1]  
a) none of these  
b) passes through z – axis  
c) parallel to z – axis  
d) perpendicular to z – axis
104. The points P  $(0, 0, 0)$ , Q  $(2, 0, 0)$ , R  $(1, \sqrt{3}, 0)$  and S  $(1, \frac{1}{\sqrt{3}}, \frac{2\sqrt{2}}{\sqrt{3}})$  lie [1]  
a) none of these  
b) in XOY plane  
c) in a line  
d) in a plane at right angles to Z – axis
105. The equation of any plane parallel to y – axis [1]  
a) none of these  
b)  $y = d$   
c)  $ax + cz = 0, a^2 + c^2 \neq 0$   
d)  $ax + cz + d = 0, a^2 + c^2 \neq 0$
106. If  $\sin x = \frac{t}{\sqrt{1+t^2}}$ , then  $\frac{dx}{dt}$  is equal to [1]  
a)  $\frac{1}{\sqrt{1-t^2}}$   
b)  $\frac{1}{1+t^2}$   
c)  $\cos x + t^2$   
d)  $\frac{1}{(1+t^2)^{3/2}}$
107.  $\frac{d}{dx} \left( \tan^{-1} \left( \frac{x}{\sqrt{1-x^2}} \right) \right)$  is equal to [1]  
a)  $\frac{1}{1+x^2}$   
b)  $\frac{-1}{\sqrt{1-x^2}}$   
c)  $1 + x^2$   
d)  $\frac{1}{\sqrt{1-x^2}}$
108. If  $f(x) = \sqrt{1-x^2}, x \in (0, 1)$ , then  $f'(x)$  is equal to [1]  
a)  $\sqrt{1-x^2}$   
b)  $\sqrt{x^2-1}$   
c)  $\frac{1}{\sqrt{1-x^2}}$   
d)  $\frac{-x}{\sqrt{1-x^2}}$
109.  $\lim_{x \rightarrow 1} \frac{1}{x} (\cos[x])$  [1]

- a) 0  
c) does not exist
110.  $\frac{d}{dx}(\sin^{-1}(1-x))$  is equal to [1]  
 a)  $\frac{-1}{\sqrt{2x-x^2}}$   
 b)  $\frac{1}{\sqrt{x^2-2x}}$   
 c)  $\frac{1-x}{(2x-x^2)^{\frac{3}{2}}}$   
 d)  $\frac{1}{\sqrt{2x-x^2}}$
111.  $\lim_{h \rightarrow 0} \frac{\sin \sqrt{x+h} - \sin \sqrt{x}}{h}$  is equal to [1]  
 a)  $\frac{1}{2 \sin \sqrt{x}}$   
 b)  $\frac{\cos \sqrt{x}}{2\sqrt{x}}$   
 c)  $\frac{\cos \sqrt{x}}{2\sqrt{x}}$   
 d)  $\sin \sqrt{x}$
112. If  $y = \sqrt{\log x + \sqrt{\log x + \sqrt{\log x + \dots to \infty}}}$  then  $\frac{dy}{dx}$  is equal to [1]  
 a)  $\frac{y}{2x-1}$   
 b)  $\frac{1}{x(2y-1)}$   
 c)  $\frac{x}{2y-1}$   
 d)  $\frac{\log x}{2y-1}$
113. If  $y = \sin^{-1} x$  and  $z = \cos^{-1} \sqrt{1-x^2}$ , then  $\frac{dy}{dz} =$  [1]  
 a) -1  
 b)  $\tan^{-1} \frac{x}{\sqrt{1-x^2}}$   
 c) 1  
 d) 0
114.  $\frac{d}{dx} \left\{ \tan^{-1} \left( \frac{3x-x^3}{1-3x^2} \right) \right\}$  is equal to [1]  
 a)  $\frac{1}{1+x^2}$   
 b)  $\sec^2 3x$   
 c)  $\frac{3}{1+x^2}$   
 d)  $\frac{3}{1+9x^2}$
115.  $\lim_{x \rightarrow 3} \frac{\sqrt{x^2+10} - \sqrt{19}}{x-3}$  is equal to [1]  
 a) 1  
 b)  $\frac{6}{\sqrt{19}}$   
 c)  $\frac{3}{\sqrt{19}}$   
 d) 0
116.  $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\sec x - \sqrt{2}}{x - \frac{\pi}{4}}$  is equal to [1]  
 a) -1  
 b) 0  
 c)  $\sqrt{2}$   
 d)  $\sqrt{3}$
117.  $\lim_{x \rightarrow \frac{\pi}{3}} \frac{\sec x - 2}{x - \frac{\pi}{3}}$  is equal to [1]  
 a) 2  
 b)  $2 + \sqrt{3}$   
 c)  $\sqrt{3}$   
 d)  $2\sqrt{3}$
118.  $\lim_{x \rightarrow 0} \frac{\sin x^n}{(\sin x)^m}, n > m > 0$ , is equal to [1]  
 a)  $\frac{m}{n}$   
 b) 0  
 c) 1  
 d)  $\frac{n}{m}$

119.  $\lim_{x \rightarrow \infty} (\sqrt{x^2 + 1} - x)$  is equal to [1]
- a) 0 b) 2  
c) -1 d)  $\frac{1}{2}$
120.  $\lim_{x \rightarrow 0} \left( \frac{\tan x - x}{x} \right) \sin\left(\frac{1}{x}\right)$  is equal to [1]
- a) 1 b) a real number other than 0 and 1  
c) -1 d) 0



## Solution

### Class 11 - Physics

#### MULTIPLE CHOICE EXAMINATION JANUARY 2019-20

##### Section A

1. (a) For small deformations the stress and strain are proportional to each other

**Explanation:** By definition of Hooke's law

within elastic limit, the stress developed is directly proportional to the strain produced in a body.

$stress \propto strain$

2. (c)  $4.8 \times 10^9$  Pa

*bulk modulus is defined as*  $B = -\frac{P}{\Delta V/V}$

*here P is volume stress which is equal to pressure*

**Explanation:** given  $P = 3.6 \times 10^6$  pa       $\Delta V = -0.45$  cm<sup>3</sup>     $V = 600$  cm<sup>3</sup>

$$B = -\frac{3.6 \times 10^6}{-0.45/600}$$

$$B = 4.8 \times 10^9 \text{ pa}$$

3. (b)  $2.2 \times 10^6$  N/m<sup>2</sup>

*bulk modulus*  $B = \frac{\Delta P}{\frac{\Delta V}{V}}$

**Explanation:** given  $V = 1$  lit    *bulk modulus*  $B = 2.2$  Gpa =  $2.2 \times 10^9$  pa

$$\Delta V = 0.10\%$$

$$\Delta P = B \times \frac{\Delta V}{V}$$

$$\Delta P = 2.2 \times 10^9 \times \frac{0.10}{100 \times 1} = 2.2 \times 10^6 \text{ N/m}^2$$

4. (b)  $2.1 \times 10^{-10}$  Pa<sup>-1</sup>

*compressibility(K) is defined as reciprocal of bulk modulus*

*bulk modulus is defined as*  $B = -\frac{P}{\Delta V/V}$

*here P is volume stress which is equal to pressure*

given  $P = 3.6 \times 10^6$  pa       $\Delta V = -0.45$  cm<sup>3</sup>     $V = 600$  cm<sup>3</sup>

**Explanation:**  $B = -\frac{3.6 \times 10^6}{-0.45/600}$

$$B = 4.8 \times 10^9 \text{ pa}$$

$$K = \frac{1}{B} = \frac{1}{4.8 \times 10^9}$$

$$K = 2.1 \times 10^{-10} \text{ pa}^{-1}$$

5. (d)  $2.18 \times 10^{-6}$

*young modulus*  $y = 2.0 \times 10^{11} \text{ N/m}^2$

*also*  $y = \frac{\text{stress}}{\text{strain}}$

*strain*  $= \frac{\text{stress}}{y} = \frac{F}{A \times y}$

*if we assume uniform distribution of weight then weight on one*

*cylinder*  $(m) = \frac{50000}{4} = 12500 \text{ kg}$

**Explanation:**

*restoring force*  $F = mg = 12500 \text{ g}$

*area of each cylinder*  $A = \pi(r_2 - r_1)^2$

$A = 3.14 \times (60 - 30)^2 \times 10^{-4} = 0.28 \text{ m}^2$

*strain*  $= \frac{12500 \times 9.8}{0.28 \times 20 \times 10^{10}}$

*strain*  $= 2.18 \times 10^{-6}$

6. (b)  $2.5 \times 10^{11} \text{ Pa}$

**Explanation:** Given compression force  $F = 50000 \text{ N}$

Radius will be  $r = \frac{\text{diameter}}{2} = \frac{0.50}{2} = 0.25 \text{ mm} = 0.25 \times 10^{-3} \text{ m}$

Area at which compression is applied  $A = \pi r^2 = 3.14 \times (0.25 \times 10^{-3})^2 = 0.2 \times 10^{-6} \text{ m}^2$

Pressure at the tip  $P = \frac{\text{Force}}{\text{area}} = \frac{50000}{0.2 \times 10^{-6}}$

$P = 2.5 \times 10^{11} \text{ pa}$

7. (d) that it enables a safe and sound design of bridges, buildings, machinery parts.

**Explanation:** More the elastic a material is , more it has the property to regain its original position which is required in construction works.

8. (d)  $1.034 \times 10^3 \text{ kg/ m}^3$

**Explanation:** Let the given depth be h.

Pressure at the given depth,  $p = 80.0 \text{ atm} = 80 \times 1.01 \times 10^5 \text{ Pa}$

Density of water at the surface,  $\rho_1 = 1.03 \times 10^3 \text{ kg m}^{-3}$

Let  $\rho_2$  be the density of water at the depth h.

Let  $V_1$  be the volume of water of mass m at the surface.

Let  $V_2$  be the volume of water of mass m at the depth h.

Let  $\Delta V$  be the change in volume.

$$\Delta V = V_1 - V_2 = m \left[ \frac{1}{\rho_1} - \frac{1}{\rho_2} \right]$$

$$\text{volumetric strain} = \frac{\Delta V}{V_1} = m \left[ \frac{1}{\rho_1} - \frac{1}{\rho_2} \right] \times \frac{\rho_1}{m}$$

$$\frac{\Delta V}{V_1} = 1 - \frac{\rho_1}{\rho_2} \rightarrow (1)$$

$$\text{bulk modulus } B = \frac{P}{\frac{\Delta V}{V_1}}$$

$$\frac{\Delta V}{V_1} = \frac{P}{B} \text{ but compressibility } \frac{1}{B} \text{ of water is } 45.8 \times 10^{-11} \text{ pa}^{-1}$$

$$\frac{\Delta V}{V_1} = 80 \times 1.013 \times 10^5 \times 45.8 \times 10^{-11} = 3.71 \times 10^{-3} \rightarrow (2)$$

from equation 1 and 2

$$1 - \frac{\rho_1}{\rho_2} = 3.71 \times 10^{-3}$$

$$\rho_2 = \frac{1.03 \times 10^3}{1 - (3.71 \times 10^{-3})}$$

$$\rho_2 = 1.034 \times 10^3 \text{ kg/m}^3$$

9. **(b)** 0.7 m from steel wire

**Explanation:** let L be the length of each of the wires A and B. Also given cross sectional area of wire

$$A_{\text{steel}}=1\text{mm}^2 \quad \text{cross sectional area of } B_{\text{al}}=2\text{mm}^2$$

$$\text{young modulus for steel } y_{\text{steel}}=200 \text{ Gpa}=2 \times 10^{11} \text{ N/m}^2$$

$$\text{young modulus of aluminium } y_{\text{al}}=70\text{Gpa}=7 \times 10^{10} \text{ N/m}^2$$

Let after placing the mass m weight on lower ends of wire be  $F_1$  and  $F_2$  then stress on wires A and B will

$$\text{be } \frac{F_1}{A_{\text{steel}}} \text{ and } \frac{F_2}{A_{\text{al}}}$$

Now given condition is stress should be equal thus

$$\frac{F_1}{A_{\text{steel}}} = \frac{F_2}{A_{\text{al}}} \Rightarrow \frac{F_1}{F_2} = \frac{A_{\text{steel}}}{A_{\text{al}}} \rightarrow (1)$$

if mass m is placed at a distance x and y from two wires then

$$F_1x = F_2y$$

$$\frac{F_1}{F_2} = \frac{y}{x} \rightarrow (2)$$

From equation 1 and 2

$$\frac{y}{x} = \frac{A_{\text{steel}}}{A_{\text{al}}} \Rightarrow x = \frac{A_{\text{al}}}{A_{\text{steel}}} y \rightarrow (3)$$

also given  $x + y = 1.05$  (total length of rod)

$$y = 1.05 - x \rightarrow (4)$$

thus from 3 and 4

$$x = \frac{A_{\text{al}}}{A_{\text{steel}}} (1.05 - x) \Rightarrow x A_{\text{steel}} = A_{\text{al}} 1.05 - A_{\text{al}} x$$

$$x (A_{\text{steel}} + A_{\text{al}}) = A_{\text{al}} \times 1.05 \Rightarrow x = \frac{2 \times 10^{-6} \times 1.05}{(2+1) \times 10^{-6}}$$

$$x = 0.7 \text{ m}$$

Thus mass should be placed 0.7m from steel wire.

10. **(d)** all the atoms or molecules are displaced from their equilibrium positions causing a change in inter atomic (or intermolecular) distances.

**Explanation:** External force permanently disturbed the equilibrium position of the interatomic ( or intermolecular ) forces between the particles of solid bodies.

11. **(d)** water will flow down the sides of the capillary tube

**Explanation:** The height of a liquid in a capillary is given by

$$h = \frac{2S \cos \theta}{r \rho g}$$

But if the capillary tube is of a length less than h the liquid does not overflow or came out if it is cut suddenly. The angle made by the liquid surface with the tube changes in such a way that force due to surface of tube on surface of liquid  $F = 2\pi rS \cos \theta$  equals the weight of the liquid raised.

12. **(b)** transmitted undiminished and equally

**Explanation:** Pascal's principle is defined as a change in pressure at any point in an enclosed fluid at rest is transmitted undiminished to all points in the fluid.

This principle is stated mathematically as:

$$\Delta P = \rho g (\Delta h)$$

$\Delta P$  is the hydrostatic pressure (given in pascals in the SI system), or the difference in pressure at two points within a fluid column, due to the weight of the fluid.

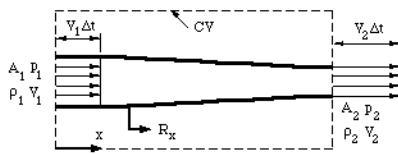
13. **(c)** adjacent layers of fluid slide smoothly past each other and the flow is steady

**Explanation:** laminar flow (or streamline flow) occurs when a fluid flows in parallel layers, with no disruption between the layers. At low velocities, the fluid tends to flow without lateral mixing, and adjacent layers slide past one another like playing cards.

14. **(a)** Lesser when the parrot flies in the cage

**Explanation:** For the bird to stay in the air, the wings must push down on the air under them. If the cage is air tight, the air exerts an equal force on the floor of the cage. The net force down on the scale will remain constant. If the cage is not air tight (i.e; the wire cage), the air will move down and horizontal. The force down will be less than the weight of the bird.

15. **(a)** will move apart rapidly  
**Explanation:** They will move apart rapidly because surface tension of oil is lesser than that of water.
16. **(b)** turbulent  
**Explanation:** When any liquid is flowing more than the velocity of its critical velocity then flow becomes turbulent.
17. **(a)** 3.0  
**Explanation:**  $W_1 = W_2$   
 $m_1 g - v_1 \rho \omega g = m_2 g - v_2 \rho \omega g$   
 $36 - 4 * 1 = 48 - V_2 * 1$   
 $V_2 = 48 - 32 = 16 m^3$   
 $\rho = m_2 / v_2 = 48 / 16 = 3 g / cm^3$
18. **(a)**  $N^{\frac{1}{3}}$   
**Explanation:** When a droplet of radius R is broken into N small droplets total volume will remain constant. Let radius of small droplets be r. Then  
 $\frac{4}{3} \pi R^3 = N \frac{4}{3} \pi r^3$   
 $r = \frac{R}{N^{\frac{1}{3}}}$   
*work done will be equal to the change in surface energy thus*  
 $W = S_f - S_i = N 4 \pi r^2 T - 4 \pi R^2 T$   
 $W = N 4 \pi \left( \frac{R}{N^{\frac{1}{3}}} \right)^2 T - 4 \pi R^2 T$   
 $W = 4 \pi R^2 T \left( N^{\frac{1}{3}} - 1 \right)$   
*if  $N^{\frac{1}{3}}$  is very large thus it becomes*  
 $W = 4 \pi R^2 T N^{\frac{1}{3}}$   
*thus*  
 $W \propto N^{\frac{1}{3}}$
19. **(c)** 125 gm  
**Explanation:**  
When it is submerged completely its weight will be balanced by the buoyant force which is equal to the mass of water displaced. Thus let mass of block be m then at equilibrium  
 $mg = V \rho g$   
 $m = 5 \times 5 \times 5 \times 1$   
 $m = 125 \text{ gm}$
20. **(d)** is that it can flow  
**Explanation:** fluids can flow due to unbalanced forces between the atoms of fluids.
21. **(b)**  $A_1 V_1 = A_2 V_2$   
**Explanation:** When a fluid is in motion, it must move in such a way that mass is conserved. Consider the steady flow of fluid through a duct (that is, the inlet and outlet flows do not vary with time). The inflow and outflow are one-dimensional, so that the velocity V and density  $\rho$  are constant over the area A.



Now we apply the principle of mass conservation. Since there is no flow through the side walls of the duct, what mass comes in over  $A_1$  goes out of  $A_2$ , (the flow is steady so that there is no mass accumulation).

Over a short time interval  $\Delta t$

Volume flow in over  $A_1 = A_1 V_1 \Delta t$

Volume flow out over  $A_2 = A_2 V_2 \Delta t$

Therefore

mass in over  $A = \rho A_1 V_1 \Delta t$

mass out over  $A = \rho A_2 V_2 \Delta t$

So:  $\rho A_1 V_1 = \rho A_2 V_2 \Delta t$

As volume is same so this equation can be written as

$$A_1 V_1 = A_2 V_2$$

This is a statement of the principle of mass conservation for a steady, one-dimensional flow, with one inlet and one outlet. This equation is called the continuity equation for steady one-dimensional flow.

22. (d) Concave

**Explanation:** Formation of meniscus depends on cohesive and adhesive forces in a liquid. For water, adhesive forces are stronger than the cohesive forces, therefore, water in a container stick to the wall of container and owing to the capillary action rises a little bit and form concave meniscus.



When liquid water is confined in a tube, its surface (meniscus) has a concave shape because water wets the surface and creeps up the side.

23. (d) 3:1

**Explanation:** Using the relation for height of liquid in a capillary tube

$$h = \frac{2S \cos \theta}{r \rho g}$$

thus if all other parameter are fixed

$$h \propto \frac{1}{r}$$

$$\Rightarrow \frac{h_1}{h_2} = \frac{r_2}{r_1} \text{ given } h_1 = 2.2 \text{ and } h_2 = 6.6$$

$$\frac{2.2}{6.6} = \frac{r_2}{r_1}$$

$$\frac{r_1}{r_2} = 3 : 1$$

24. (c) equal to the upward buoyant force

**Explanation:** This is archimedes principle when an object submerged in a liquid its weight is equal to the Buoyant force.

25. (b) 2d

**Explanation:** Density of mixture is given by

$$\rho_{mix} = \frac{\text{total mass}}{\text{total volume}} = \frac{m_1 + m_2 + m_3}{v_1 + v_2 + v_3}$$

as  $v_1 = v_2 = v_3$

$$\rho_{mix} = \frac{\rho_1 v + \rho_2 v + \rho_3 v}{v + v + v}$$

$$\Rightarrow \frac{d v + 2d v + 3d v}{3v}$$

$$\rho_{mix} = 2d$$

26. (d) 18/11d

**Explanation:** Density of mixture of liquids is given by

$$\rho_{mix} = \frac{\text{total mass}}{\text{total volume}} = \frac{m_1 + m_2 + m_3}{\frac{m_1}{\rho_1} + \frac{m_2}{\rho_2} + \frac{m_3}{\rho_3}}$$

$$\rho_{mix} = \frac{\frac{x}{3} + \frac{x}{3} + \frac{x}{3}}{\frac{x}{3d} + \frac{x}{6d} + \frac{x}{9d}}$$

$$\rho_{mix} = \frac{18d}{11}$$

27. (b) 0.47

**Explanation:** V = Volume of metal

V' = Volume of mercury displaced

Weight of body = Weight of mercury displaced

$$= 7.2 \times 9810 \times V = 13.6 \times 9810 \times V'$$

$$\Rightarrow \frac{V'}{V} = 0.53$$

Fraction of volume above mercury = 1 - 0.53 = 0.47

28. (b) Addition of soap to water decreases surface tension of water

**Explanation:** Addition of soap decreases the surface tension of water, as we know the energy of spraying is directly proportional to the surface tension.

29. (d) 54.88 N

**Explanation:** Water compartment,

$$P = h\rho g$$

$$= 4 \times 1.0 \times 10^3 \times 9.8$$

$$= 39.2 \times 10^3 \text{ Pa}$$

Acid Compartment,

$$P' = h\rho'g$$

$$= 4 \times 1.7 \times 10^3 \times 9.8$$

$$= 66.64 \times 10^3 \text{ Pa}$$

Now,

$$P' - P = 66.64 \times 10^3 - 39.2 \times 10^3$$

$$P' - P = 27.44 \times 10^3 \text{ Pa}$$

$$A = 20 \text{ cm}^2 = 20 \times 10^{-4} \text{ m}^2$$

Force using pressure,

$$\text{Pressure} = \frac{\text{Force}}{\text{Area}}$$

$$\text{Force} = \text{pressure} \times \text{area}$$

$$F = 27.44 \times 10^3 \times 20 \times 10^{-4}$$

$$F = 54.88 \text{ N}$$

30. (d)  $\frac{A_2}{A_1} F_1$

**Explanation:** According to Pascal's Law,

Pressure applied to any point inside the liquid is transmitted equally in all directions so,

Pressure applied on the smaller cylinder is equal to the pressure on the other cylinder, which is given by

$$\frac{F_1}{A_1} = \frac{F_2}{A_2}$$

So,

Maximum force on the other side is,

$$F_2 = \frac{A_2}{A_1} \times F_1$$

31. (d) Newtons per meter

**Explanation:** surface tension is measured in force per unit length. The S.I unit is newton per meter but the

CGS unit dyne per centimeter is also used.

32. (c)  $l = h \cos \alpha$

**Explanation:** This will form a right angled triangle with base  $l$  and hypotenuse  $h$  and angle between base and hypotenuse is

$\alpha$

$$\text{thus } \cos \alpha = \frac{l}{h}$$

$$l = h \cos \alpha$$

33. (d)  $\rho g (h + H) + \frac{2T}{r}$

**Explanation:** Excess pressure in a air bubble is given by

$$P_2 - P_1 = \frac{2T}{r}$$

$T \rightarrow$  surface tension  $r \rightarrow$  radius of bubble

if the bubble is at a depth  $h$  inside then

$$P_1 = P_{atm} + h\rho g$$

given  $P_{atm} = H\rho g$

$$P_1 = \rho g (H + h)$$

thus

$$P_2 = \rho g (h + H) + \frac{2T}{r}$$

34. (c)  $12\pi r^2 T$

**Explanation:**

Surface energy is given by

$S =$  surface area( $A$ )  $\times$  surface tension( $T$ )

initial surface energy

$$S_1 = 4\pi r^2 T$$

now if diameter is doubled radius will also be doubled thus surface energy will be

$$S_2 = 4\pi (2r)^2 T$$

$$S_2 = 16\pi r^2 T$$

thus excess energy required is

$$\Delta S = S_2 - S_1$$

$$\Delta S = 16\pi r^2 T - 4\pi r^2 T$$

$$\Delta S = 12\pi r^2 T$$

35. (a) pressure in a fluid at rest is the same at all points if they are at the same height

**Explanation:** According to Pascal's Law,

$$P - P_0 = h\rho g$$

from above

Change in pressure is directly proportional to depth from the free surface.

At the same horizontal line all points are at the same depth and have same value of acceleration due to gravity and density of water as well.

36. (c) a curve whose tangent at any point is in the direction of the fluid velocity at that point

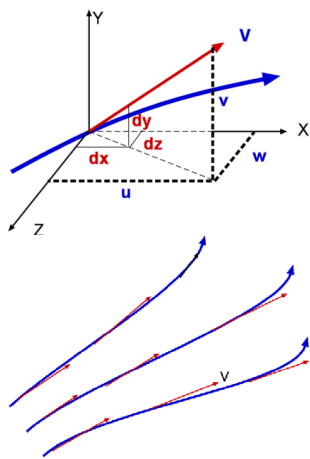
**Explanation:** Streamlines, streaklines and pathlines are field lines in a fluid flow. They differ only when the flow changes with time, that is when the flow is not steady. Considering a velocity vector field in three-dimensional space in the framework of continuum mechanics, we have that:

Streamlines are a family of curves that are instantaneously tangent to the velocity vector of the flow. These show the direction in which a massless fluid element will travel at any point in time

A streamline is one that drawn is tangential to the velocity vector at every point in the flow at a given instant and forms a powerful tool in understanding flows. This definition leads to the equation for

streamlines.  $\frac{du}{u} = \frac{dv}{v} = \frac{dw}{w}$

where  $u$ ,  $v$ , and  $w$  are the velocity components in  $x$ ,  $y$  and  $z$  directions respectively as sketched.



37. (c) 80kg

**Explanation:** Given mass of raft  $M=120$  k.g.

density of raft  $=600$  k.g./ $m^3$

thus volume of raft  $V =$

$$V = \frac{\text{Mass}}{\text{density}} = \frac{120}{600} = 0.2m^3$$

when raft just sink inside after placing extra mass  $m$ . thus weight of (raft + extra mass  $m$ )

will be equal to buoyant force. so

$$(M + m)g = V\rho g$$

$$120 + m = 0.2 \times 1000$$

$$m = 80 \text{ kg.}$$

38. (d) Transmitted unchanged to every portion of the fluid and walls of the containing vessel

**Explanation:** According to Pascal's law (or the principle of transmission of fluid-pressure) is a principle in fluid mechanics that states that a pressure change occurring anywhere in a confined incompressible fluid is transmitted throughout the fluid such that the same change occurs everywhere.

39. (d) 10 cm

**Explanation:** Let the side of the cube be  $x$ , density of water be  $\rho$ , mass of cube be  $m$ , acceleration due to gravity be  $g$ .

When the weight is on the block,

Using Archimedes' Principle ,

Weight of the block + Weight of the mass = Buoyant force ( $B_1$ )

Since Buoyant force is equal to volume of liquid displaced by body thus

$$B_1 = \rho g x^3$$

$$\text{thus } (m + 200)g = \rho g x^3$$

$$m = \rho x^3 - 200 \rightarrow (1)$$

when mass is removed the wooden cube is 2cm outside

thus volume of cube inside = volume of water displaced =  $(x - 2)x^2$

again balance the buoyant force  $B_2 = \rho g (x - 2)x^2$

$$\rho g (x - 2)x^2 = mg$$

$$\Rightarrow \rho (x - 2)x^2 = m$$

substitute for  $m$

$$\rho (x - 2)x^2 = \rho x^3 - 200$$

$$\Rightarrow 2\rho x^2 = 200$$

take  $\rho = 1 \text{ gram/cm}^3$

$$\Rightarrow x = 10 \text{ cm}$$



40. **(b)** mass per unit volume

**Explanation:** Density is defined as the compactness of substance.

Mathematically,

$$\text{Density}(D) = \frac{\text{Mass}(M)}{\text{Volume}(V)}$$

## Solution

### Class 11 - Chemistry

#### MULTIPLE CHOICE EXAMINATION JANUARY 2020

##### Section A

41. **(d)** Portland cement  
**Explanation:** Heating a pulverised mixture of limestone and clay in a rotary kiln is used in the manufacture of Portland cement. Cement is a product obtained by combining a material rich in lime, CaO with other material such as clay which contains silica, SiO<sub>2</sub> along with the oxides of aluminium, iron and magnesium.
42. **(c)**  $Be^{2+} > Mg^{2+} > Ca^{2+} > Sr^{2+} > Ba^{2+}$   
**Explanation:** As we move down the group ionic radii increases.
43. **(c)** BaCO<sub>3</sub>  
**Explanation:** BaCO<sub>3</sub> is very stable due to size compatibility factor. A larger cation can stabilise a larger anion. Group 2 element become more thermally stable down the group.
44. **(a)** It is used in the preparation of bleaching powder  
**Explanation:** Ca(OH)<sub>2</sub> is a white amorphous powder which is used in the manufacture of bleaching powder. It is used in white wash because of its disinfectant nature.
45. **(d)** Be(OH)<sub>2</sub>  
**Explanation:** Be(OH)<sub>2</sub> is soluble in NaOH. Since Be act as amphoteric unlike other group 2 elements
46. **(b)** High lattice enthalpy  
**Explanation:** LiF has very high lattice energy which cannot be compensated by Hydration Energy.
47. **(c)** Na<sub>2</sub>CO<sub>3</sub>  
**Explanation:** Sodium carbonate i.e. Na<sub>2</sub>CO<sub>3</sub> is used in paper, paints and textile industries.
48. **(c)** Exceptionally small size of its atom  
**Explanation:** The anomalous behaviour of lithium is due to the : (i) exceptionally small size of its atom and ion, and (ii) high polarising power (i.e., charge/ radius ratio). As a result, there is increased covalent character of lithium compounds which is responsible for their solubility in organic solvents.
49. **(b)** low ionization enthalpies  
**Explanation:** The reason is that the atoms of alkali metals are of large sizes. therefore, the outermost electron is far away from the nucleus and can be easily removed
50. **(b)** Calcium  
**Explanation:** Cement is the important compound of Calcium. Cement is a product obtained by combining a material rich in lime, CaO with other material such as clay which contains silica, SiO<sub>2</sub> along with the oxides of aluminium, iron and magnesium.
51. **(a)** The electrons in magnesium are too strongly bound to get excited  
**Explanation:** Electrons in Mg are held closer to nucleus as it is very small in size. So does not get excited by the energy provided by flame.
52. **(d)** KO<sub>2</sub>  
**Explanation:** KO<sub>2</sub> is super oxide
53. **(d)** Li  
**Explanation:** Li reacts with water least vigorously, since the density of Li is only about half that of water, so it floats on the surface and ultimately disappears, giving off H<sub>2</sub> gas
54. **(c)** Cs  
**Explanation:** Cs is stimulated by direct sun light, and in photoelectric cell, these electrons flow to create an electric current
55. **(b)** magnesium  
**Explanation:** Due to their nearly same polarizing power

56. **(a)** Cs  
**Explanation:** Size of Cs is the biggest thus its melting point is the lowest  $28.5^{\circ}\text{C}$
57. **(a)** Lithium and magnesium  
**Explanation:**  $1^{st}$  element of  $1^{st}$  group and the second element of  $2^{nd}$  group exist in diagonal relationship. Due to their nearly same polarizing power
58. **(d)** Be  
**Explanation:** Beryllium oxide (BeO) can act as an acidic as well as basic oxide. BeO is essentially covalent in nature. BeO is amphoteric while oxides of other group 2 elements are ionic in nature.
59. **(a)** hydration enthalpy decreases down the group  
**Explanation:** Solubility of sulphates and carbonates decreases down the group because of decrease in hydration energy. which is insufficient to overcome the lattice energy of ions.
60. **(a)**  $\text{Mg}^{2+}$  ions  
**Explanation:** When hard water containing  $\text{Mg}^{2+}$  &  $\text{Ca}^{2+}$  is passes through a bed of sodium zeolite, the sodium ions are replaced with by the calcium and magnesium ions. This is used in water softening process
61. **(a)** Groups 7, 8, 9  
**Explanation:** Elements of group 7, 8, 9 of d – block do not form hydrides at all. This inability of metal, of group 7, 8, 9 of periodic table to form hydrides is referred to as hydride gap of d – block.
62. **(a)**  $\text{H}_3\text{O}^+$  and  $\text{OH}^-$   
**Explanation:** Water molecules collide with one another to cause the self-ionization reaction represented by this equation:  

$$2\text{H}_2\text{O} \rightleftharpoons \text{H}_3\text{O}^+ + \text{OH}^-$$
It is a reversible reaction so the equation is usually written with the arrows going in both directions. The reaction does not form very much  $\text{H}_3\text{O}^+$  or  $\text{OH}^-$ . In one liter of water there are about 55 moles of water molecules, but only  $1.0 \times 10^{-7}$  moles of  $\text{H}_3\text{O}^+$  and  $\text{OH}^-$  are formed (at room temperature). So the concentrations of  $\text{H}_3\text{O}^+$  and  $\text{OH}^-$  in pure water are  $1.0 \times 10^{-7}$  M.
63. **(c)** an oxidising agent in (A) and reducing agent in (B)  
**Explanation:**  $\text{H}_2\text{O}_2$  is an oxidizing agent in 1st reaction and Reducing agent in 2nd reaction.
64. **(b)**  $2\text{I}^- + 2\text{H}^+ + \text{H}_2\text{O}_2 \rightarrow \text{I}_2 + 2\text{H}_2\text{O}$   
**Explanation:**  $\text{I}^-$  gets oxidized to  $\text{I}_2$  in presence  $\text{H}_2\text{O}_2$  which itself get reduced to  $\text{H}_2\text{O}$ .
65. **(b)** Heavy water is used as a moderator in nuclear reactor.  
**Explanation:** Heavy water is used in certain types of nuclear reactors, where it acts as a neutron moderator to slow down neutrons so that they are more likely to react with the fissile uranium-235 than with uranium-238, which captures neutrons without fissioning.
66. **(c)**  $\text{CaCO}_3 \cdot \text{Mg}(\text{OH})_2$   
**Explanation:**  $\text{CaCO}_3 \cdot \text{Mg}(\text{OH})_2$  can be precipitate out in order to remove temporary hardness.
67. **(a)** vanaspati  
**Explanation:** Vanaspati ghee is manufactured from vegetable or seed oil by a process called 'hydrogenation'.  
Vegetable Oil is a viscous liquid, and contains unsaturated fatty acids, upon hydrogenation it is converted to saturated fatty acids to form vanaspati ghee which is solid/semi solid in nature. For quick and easy hydrogenation, catalyst like Ni, Pt which are capable of adsorbing hydrogen are used.
68. **(a)** it breaks the chemical bonds of the chromophores  
**Explanation:** Because it can undergo bond dissociation randomly in presence of light. It dissociates and generates free radicals which is very reactive and acts like bleaching agent.
69. **(d)** Water gas  
**Explanation:** Water gas is a combustion fuel containing carbon monoxide (CO) and hydrogen gas ( $\text{H}_2$ ).  
Water gas is made by passing steam over heated hydrocarbons.

The water-gas shift reaction can be used to reduce carbon dioxide levels and enrich hydrogen content, making water gas.

70. **(d)** neutral

**Explanation:** Cation exchange resin have exchangeable hydrogen ions which makes the water acidic while anion exchange resin have exchangeable hydroxide ion which makes the water basic. Passing water to anion exchange resin as a second process after passing through anion exchange resin makes the water neutral.

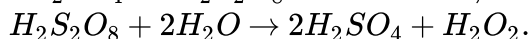
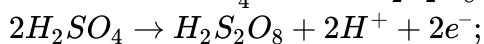
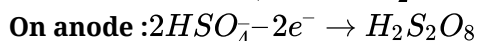
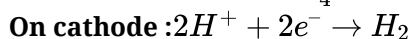
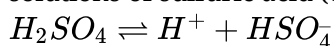
71. **(a)** all of these

**Explanation:** Hydrogen peroxide ( $H_2O_2$ ) is a very pale blue liquid which appears colourless in a dilute solution, slightly more viscous than water. It is a weak acid. It has strong oxidizing properties and is therefore a powerful bleaching agent that is mostly used for bleaching paper, but has also found use as a disinfectant and as an oxidizer.

Hydrogen peroxide in acid solution is oxidized with  $KMnO_4$  and reduced with  $KI$ . When  $H_2O_2$  serves as an oxidizing agent, the oxygen is reduced to  $H_2O$ . When  $H_2O_2$  serves as a reducing agent, the oxygen is oxidized to  $O_2$  and bubbles are noticed.

72. **(d)** sulphuric acid

**Explanation:** Hydrogen peroxide is manufactured in large amounts by the electrolysis of aqueous solutions of sulfuric acid (or of potassium bisulfate or ammonium bisulfate):



73. **(b)**  $Ca^{2+}$  ions

**Explanation:** Zeolites are characteristically soft to moderately hard, light in density, insoluble in water but can act as base exchangers in contact with water containing cations. Hence these can remove  $Ca^{2+}$  ions from water when hard water is passed through them.

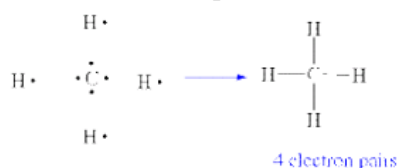
74. **(b)** It can lose an electron to form a cation which can freely exist

**Explanation:**  $H^+$  cannot exist freely due to its small size.

75. **(d)**  $CH_4$

**Explanation:** Electron precise hydride is the type of hydride in which the number of electrons present is equal to the number of electrons required (octet or duplet). For example-  $CH_4$

$CH_4$  has no lone pair of electron or vacant orbital so it is an electron precise hydride.



76. **(b)** Hydrated sodium aluminium silicate

**Explanation:** Zeolites are microporous, aluminosilicate minerals commonly used as commercial adsorbents and catalysts.

Average chemical composition of sodium zeolite is reported as Sodium Oxide - 17%, Aluminum Oxide - 28%, Silicon dioxide - 33% and water - 22%.

The formula of sodium zeolite may be represented by  $NaAlSi_2O_6 \cdot H_2O$ . Another name for this substance is hydrated sodium aluminum silicate.

77. **(a)** provides thermal insulation

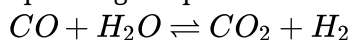
**Explanation:** Since there is no heat flux, ice once formed grows quickly on the surface of lake. As this cover completely on the surface, the snow on the ice insulate the water from the atmosphere.

Due to this the rate of ice growth is slowed down. The heat lost from the water to the atmosphere must be taken from the latent heat released when ice is formed, since the water just below the ice is at the freezing

point. Due to this thermal insulation, water at the bottom of the lake does not freeze or the thickness of ice decreases on moving down the lake. Thus the aquatic animals and plant survive.

78. **(d)** Water-gas shift reaction

**Explanation:** The water gas shift reaction converts carbon monoxide and water to carbon dioxide and hydrogen. The reaction is catalysed by a number of different base metal catalysts, depending on the operating temperature and levels of poisons in the feedstock.



79. **(a)** Manufacturing of caustic soda

**Explanation:** The chloralkali process (also chlor-alkali and chlor alkali) is an industrial process for the electrolysis of NaCl. It is the technology used to produce chlorine and sodium hydroxide (lye/caustic soda), which are commodity chemicals required by industry.

Usually the process is conducted on a brine (an aqueous solution of NaCl), in which case NaOH, hydrogen, and chlorine result.

In remaining three processes, hydrogen is a main product.

80. **(c)**  $LiH < NaH < KH < RbH < CsH$

**Explanation:** As the size of cation increases ionic character also increases.

## Solution

### Class 11 - Mathematics

#### Multiple Choice Questions Examination January (2019-20)

#### Section A

81. (d)  $\frac{3}{5}$

**Explanation:** here  $c=3$ ,  $b=4$ , from relation  $a^2=b^2+c^2$  we get  $a=5$ .  
 $e=c/a = 3/5$

82. (b) on the line  $y = x$

**Explanation:** point of intersection is  $(0,0)$  and  $(4,4)$ . This implies  $y = x$ . Hence it intersects the line  $y = x$

83. (a)  $y - a = 0$

**Explanation:** From the equation we infer that the parabola is open downward.  
Hence the directrix passes through the point  $(0,a)$  and will be parallel to the X-axis.  
Hence the equation of the directrix is  $y = a$  or  $y - a = 0$

84. (d) an ellipse

**Explanation:** The given equation can be written of the form

$$(x-9/2)^2 + 3(y+1/3)^2 - \frac{81}{4} - \frac{1}{3} + 1 = 0, \text{ i.e.; } (x-9/2)^2 + 3(y+1/3)^2 = 235$$

$$\text{That is } \frac{(x-9/2)^2}{235} + 3 \frac{(y+2/3)^2}{235} = 1$$

This is an equation of an ellipse.

85. (b)  $\sqrt{\frac{2}{3}}$

**Explanation:**  $2b^2/a^2 = 2a/3$

Hence  $\frac{b^2}{a^2} = 1/3$ . Hence  $e^2 = 1 - \frac{b^2}{a^2} = 1 - (1/3) = 2/3$

Therefore  $e = \sqrt{\frac{2}{3}}$

86. (a)  $\frac{5}{4}$

**Explanation:** Given  $9x^2 - 16y^2 = 144$

Dividing throughout by 144 we get,

$$\frac{x^2}{16} - \frac{y^2}{9} = 1$$

This implies  $a^2 = 16$  and  $b^2 = 9$

$$e = \frac{\sqrt{a^2+b^2}}{a} = \frac{5}{4}$$

87. (c)  $\sqrt{\frac{31}{12}}$

**Explanation:** The general form of the given circle is  $x^2 + y^2 - 2x + y - 4/3 = 0$

Hence  $g = 1$ ,  $f = -1/2$  and  $c = -4/3$

$$\text{Radius} = \sqrt{g^2 + f^2 - c}$$

Substituting the values we get,

$$\text{Radius} = \sqrt{1 + 1/4 + 4/3} = \sqrt{\frac{31}{12}}$$

88. (b) none of these.

**Explanation:** If  $a^2 = b^2$ , then the equation becomes  $x^2 + y^2 = a^2$  which represents the equation of a circle.

89. (c)  $(\frac{1}{2}, -\sqrt{2})$

**Explanation:** Since the circle passes through  $(0,0)$  the equation reduces to  
 $c = 0$  ----(1)

Since it passes through  $(1,0)$ ,

$$1 + 2g + c = 0$$

This implies  $g = -1/2$

Since the circle touches the circle  $x^2 + y^2 = 9$ , their radii should be equal

$$2\sqrt{g^2 + f^2 + c} = 3$$

Substituting the values and simplifying we get  $f = \pm\sqrt{2}$

Hence the centre is  $(1/2, -\sqrt{2})$

90. (c) Equal to 1

**Explanation:** Eccentricity of a parabola is 1

91. (b) an ellipse

**Explanation:** parametric form of ellipse.

92. (b)  $(-a, 0)$

**Explanation:** Let the equa  $y = Y$  and  $(x+a) = X$

Then the equation of the parabola can be written as

$$Y^2 = 4aX, \text{ whose vertex is } (0,0)$$

Therefore  $x+a=0$  and  $y=0$ , implies  $x = -a$  and  $y = 0$

Hence the vertex of the given parabola is  $(-a,0)$

93. (c)  $\sqrt{2}$

**Explanation:**  $x^2 - y^2 = 9$

above equation can be written as,

$$\frac{x^2}{(3)^2} - \frac{y^2}{(3)^2} = 1$$

comparing it with the standard equation we get  $a=3$  and  $b=3$

$$\text{as } c = \sqrt{a^2 + b^2}$$

$$\text{we get } c = 3\sqrt{2}$$

$$\text{and as } e = \frac{c}{a}$$

$$\text{we get } e = \sqrt{2}$$

94. (b)  $\frac{2\sqrt{2}}{3}$

**Explanation:** here  $b/a=1/3$

$$\text{Hence } \frac{b^2}{a^2} = \frac{1}{9}, b^2 = \frac{a^2}{9}$$

$$\text{Therefore } b^2 = a^2(1 - e^2)$$

Substituting the values we get

$$e = \frac{2\sqrt{2}}{3}$$

95. (d) 4

**Explanation:**  $\frac{x^2}{16} + \frac{y^2}{9} = 1$

comparing with the standard equation we get  $a=4$  and  $b=3$  we get  $c = \sqrt{16 - 9} = \sqrt{7}$

so focus is  $(\sqrt{7}, 0)$  and the given centre is  $(0,3)$ .

using distance formulae. we get radius = 4 units

96. (d) the X axis

**Explanation:** The equation  $\vec{r} = \lambda \hat{i}$  represents X-axis

**Explanation**  $-\vec{r} = \lambda \hat{i}$

$$\vec{r} = x\hat{i} + y\hat{j} + z\hat{k} = \lambda\hat{i} + 0\hat{j} + 0\hat{k}$$

$x = \lambda, y = 0, z = 0$  this is a general point on X axis, So given equation represents X axis

97. (b)  $x = 0, z = 0$

**Explanation:** Since on Y axis  $x$  and  $z$  coordinate are 0.

So, Equations of Y axis are  $X=0$  and  $Z=0$

98. (b) coplanar

**Explanation:**  $\vec{a} = 1\hat{i} + 1\hat{j} + 0\hat{k}, \vec{b} = (0\hat{i} + 1\hat{j} + 1\hat{k}), \vec{c} = ((\hat{i} + 0\hat{j} + 1\hat{k}), \vec{d} = (2/3\hat{i} + 2/3\hat{j} + 2/3\hat{k})$

$$\vec{AB} = -1\hat{i} + 0\hat{j} + 1\hat{k}, \vec{AC} = -0\hat{i} + -1\hat{j} + 1\hat{k}, \vec{AD} = -1/3\hat{i} + -1/3\hat{j} + 2/3\hat{k}$$

$$\text{Consider } \begin{vmatrix} -1 & 0 & 1 \\ 0 & -1 & 1 \\ -1/3 & -1/3 & 2/3 \end{vmatrix} = -1(-1/3) + 1(-1/3)$$

=0

Hence points are coplanar

99. (b) 1/3

**Explanation:** since XOZ plane is given y coordinate must be zero

$$k \times 3 + 1 \times (-1) / k + 1 = 0$$

$$3k - 1 = 0$$

$$k = 1/3$$

100. (d) it is -2 : 3

**Explanation:** The ratio in which the line joining (2, 4, 5) (3, 5, -4) is divided by the YZ - plane is

Point in YZ plane will be P(0, y, z) let it divides the line joining points A(2, 4, 5) and B(3, 5, -4) in the ratio k : 1

then X coordinate of point P will be given by  $\frac{3k+2}{k+1}$  which is equal to zero

$$\text{i.e. } \frac{3k+2}{k+1} = 0 \Rightarrow 3k+2=0 \Rightarrow k = -2/3$$

so, YZ plane divides in -2 : 3

101. (d)  $\frac{\sqrt{155}}{2}$

**Explanation:** let  $\vec{a} = (1\hat{i} + 2\hat{j} + 3\hat{k}), \vec{b} = (2\hat{i} + 5\hat{j} - 1\hat{k}), \vec{c} = (-1\hat{i} + 1\hat{j} + 2\hat{k})$

$$\text{Area of triangle} = \frac{1}{2} [\vec{a} * \vec{b} + \vec{b} * \vec{c} + \vec{c} * \vec{a}]$$

$$= \frac{1}{2} \left[ \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 3 \\ 2 & 5 & -1 \end{vmatrix} + \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 5 & -1 \\ -1 & 1 & 2 \end{vmatrix} + \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -1 & 1 & 2 \\ 1 & 2 & 3 \end{vmatrix} \right]$$

$$= \frac{1}{2} [-17\hat{i} + 7\hat{j} + 1\hat{k} + 11\hat{i} - 3\hat{j} + 7\hat{k} - 1\hat{i} + 5\hat{j} - 3\hat{k}]$$

$$= \frac{1}{2} [-7\hat{i} + 9\hat{j} + 5\hat{k}]$$

$$\text{Area} = \frac{1}{2} \sqrt{49 + 81 + 25}$$

$$\text{Area} = \sqrt{155}/2$$

102. (c) an equilateral triangle

**Explanation:** To check which type of triangle these points form we need to check the distance between the two points

$$AB = \sqrt{(\sqrt{3})^2 + 1 + 0} = 2$$

$$BC = \sqrt{\left(\frac{1}{\sqrt{3}} - \sqrt{3}\right)^2 + \left(\frac{2\sqrt{2}}{\sqrt{3}}\right)^2} = 2,$$

similarly AC=2 by distance formula between two points

Since all sides are same so the triangle is equilateral

103. (b) passes through z - axis

**Explanation:**

Co - ordinates of any point on z - axis are (0, 0, z)

∴ The plane  $x + y = 0$  will pass through z - axis if (0, 0, z) satisfies  $x + y = 0$  .....(1)

Now L.H.S of (1) =  $x + y$

For (0, 0, z), L.H.S of (1) =  $0 + 0 = 0 =$  R.H.S of (1)

Hence the result

104. (a) none of these

**Explanation:** The equation of plane passing through (0,0,0) is  $a(x-0)+b(y-0)+c(z-0)=0$

$ax+by+cz=0$ .if it passes through Q (2, 0, 0), R (1,  $\sqrt{3}$ , 0) then we get

$$2a=0; a+\sqrt{3}b=0 \text{ i.e. we get } a=0 \text{ and } b=0$$

Now if we put co-ordinates of S it does not satisfy the equation.

hence points are not coplanar



105. (d)  $ax + cz + d = 0, a^2 + c^2 \neq 0$

**Explanation:** Since the plane  $ax+by+cz+d=0$  is parallel to  $y$  axis hence  $b=0$ .  
hence  $ax+cz+d=0$ .

106. (b)  $\frac{1}{1+t^2}$

**Explanation:** we have,

$$x = \sin^{-1} \frac{t}{\sqrt{1+t^2}}$$

$$\text{let } t = \tan \theta$$

$$\Rightarrow x = \theta \Rightarrow \frac{dx}{d\theta} = 1$$

$$\text{Also, } \frac{dt}{d\theta} = \sec^2 \theta$$

$$\text{Now, } \frac{dx}{dt} = \frac{1}{\sqrt{1+t^2}}$$

107. (d)  $\frac{1}{\sqrt{1-x^2}}$

**Explanation:** Substitute  $x = \sin \theta; \frac{dx}{d\theta} = \cos \theta$

$$\Rightarrow y = \theta$$

$$\Rightarrow \frac{dy}{dx} = \sec \theta$$

$$\Rightarrow \frac{1}{\sqrt{1-x^2}}$$

108. (d)  $\frac{-x}{\sqrt{1-x^2}}$

**Explanation:**  $f'(x) = \frac{1}{2\sqrt{1-x^2}} \cdot -2x$

109. (c) does not exist

**Explanation:**  $R.H.L = \lim_{x \rightarrow 1^+} (\cos[x]) = \cos 1$

$$L.H.L. = \lim_{x \rightarrow 1^-} (\cos[x]) = \cos 0 = 1$$

Since  $L.H.L. \neq R.H.L.$  therefore limit does not exist.

110. (c)  $\frac{1-x}{(2x-x^2)^{\frac{3}{2}}}$

**Explanation:**  $y = \sin^{-1}(1-x)$

$$\Rightarrow \sin y = 1-x$$

$$\Rightarrow (\cos y)y' = -1$$

$$\Rightarrow y'' = (y')^2 (\tan y) = \frac{(\sin y)}{(\cos y)^3}$$

$$\Rightarrow \frac{1-x}{(2x-x^2)^{\frac{3}{2}}}$$

111. (c)  $\frac{\cos \sqrt{x}}{2\sqrt{x}}$

**Explanation:**  $\lim_{h \rightarrow 0} \frac{2 \cos(\frac{\sqrt{x+h}+\sqrt{x}}{2}) \sin(\frac{\sqrt{x+h}-\sqrt{x}}{2})}{h}$

using L'Hospital

$$\Rightarrow \frac{\cos \sqrt{x}}{2\sqrt{x}}$$

112. (b)  $\frac{1}{x(2y-1)}$

**Explanation:**  $y = \sqrt{\log x + y}$

$$y^2 = \log x + y$$

$$2yy' = \frac{1}{x} + y'$$

$$y' = \frac{1}{(x)(2y-1)}$$

113. (c) 1

**Explanation:** we have;

$$\begin{aligned} \sin y = x \text{ and } \cos z = \sqrt{1-x^2} &\implies \cos z = \cos y \\ \implies z = y \\ \implies \frac{dy}{dz} = 1 \end{aligned}$$

114. (c)  $\frac{3}{1+x^2}$

**Explanation:** Substitute  $x = \tan \theta$ ;  $\frac{dx}{d\theta} = \sec^2 \theta$

$$\begin{aligned} \implies y = 3\theta \\ \implies \frac{dy}{dx} = 3 \cos^2 \theta = \frac{3}{1+x^2} \end{aligned}$$

115. (c)  $\frac{3}{\sqrt{19}}$

**Explanation:** Using L'Hospital,  $Lt_{x \rightarrow 3} \frac{\frac{2x}{2\sqrt{x^2+10}}}{1}$

$$\begin{aligned} \text{Substituting } x = 3 \text{ in } \frac{\frac{2x}{2\sqrt{x^2+10}}}{1} \\ \text{we get} \\ \frac{3}{\sqrt{19}} \end{aligned}$$

116. (c)  $\sqrt{2}$

**Explanation:** Using L'Hospital;

$$\begin{aligned} Lt_{x \rightarrow \frac{\pi}{4}} \frac{\sec x \tan x}{1} \\ \implies \sqrt{2} \end{aligned}$$

117. (d)  $2\sqrt{3}$

**Explanation:** Using L'Hospital;

$$\begin{aligned} Lt_{x \rightarrow \frac{\pi}{3}} \frac{\sec x \tan x}{1} \\ \implies 2\sqrt{3} \end{aligned}$$

118. (b) 0

$$\begin{aligned} \text{Explanation: } Lt_{x \rightarrow 0} \frac{\sin x^n}{(\sin x)^m} \cdot \frac{x^{m+n}}{x^{m+n}} \\ \implies Lt_{x \rightarrow 0} \frac{\sin x^n}{x^n} \cdot \frac{x^m}{(\sin x)^m} \cdot \frac{x^n}{x^m} \\ \implies 1 \cdot 1^m \cdot x^{n-m} \\ \implies 1 \cdot 0 = 0 \end{aligned}$$

119. (a) 0

**Explanation:** Put  $x = \frac{1}{t}$

$$\text{Then, } Lt_{t \rightarrow 0} \frac{(\sqrt{1+t^2}-1)}{t}$$

$$\text{Applying L'Hospital } Lt_{t \rightarrow 0} \frac{\frac{2t}{2\sqrt{1+t^2}}}{1} = 0$$

120. (d) 0

$$\begin{aligned} \text{Explanation: } Lt_{x \rightarrow 0} \left( \frac{\tan x}{x} - \frac{x}{x} \right) \sin\left(\frac{1}{x}\right) \\ \implies 0 \cdot \text{Finite number} = 0 \end{aligned}$$